# A Stochastic General Equilibrium Model with Partial Dollarization

Paul Castillo, Carlos Montoro and Vicente Tuesta
"Foreign Currency Related Risk Taking by Financial Institutions, Firms and
Households"

Central Reserve Bank of Peru

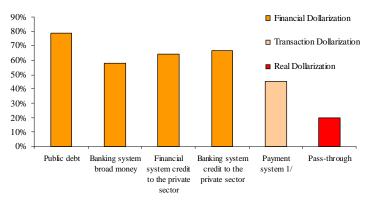
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Types of Partial Dollarization

**Definition:** Partial replacement of the domestic currency by a foreign currency (i.e. US dollars) in its basic functions

- Currency Substitution (CS): Dollars accepted as a medium of payment
- Price Dollarization (PD): Prices are indexed to changes in the exchange rate
- Financial Dollarization (FD): Dollars are used as a store of value

Peru is one of the most highly dollarized economies + IT



Other LA countries: Bolivia, Nicaragua, Paraguay and Uruguay.

Why dollarization is important for policy makers?

- Limitations of the Central Bank in stabilizing inflation and output
- Transmission mechanism of monetary policy: Demand and supply side effects of dollarization.
- Affects objectives of the central bank: Exchange rate smoothing versus interest rate smoothing.
- Regulatory and prudential issues: currency mismatches and balance-sheet effects.

#### Goal of the Paper

- To develop a DSGE model with partial dollarization to understand the transmission mechancism.
- Use the model to account for the effects of partial dollarization.
- Estimate the model using Bayesian techniques.
- Policy evaluation (MEGA-D).

What do we do?

- Add to a standard sticky price SOE model 3 forms of partial dollarization: CS, PD and FD
- Estimate the model using Bayesian Methods and Peruvian data
- Use the model for policy analysis (forecast).

#### Main ingredients

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- Exchange rate intervention.

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- Exchange rate intervention: Bofinger y Wollmershäuser (2003), Adolfson et.al. (2007, Riskbank), Florian, Salas and Vega (2007): intervention affects risk premium in the UIP.

# Extension 1: Currency substitution

$$U\left(C_{t}^{j}\right) = \xi_{t}\log\left\{\left[b\left(C_{t}^{j} - hC_{t-1}\right)^{\frac{\omega-1}{\omega}} + (1-b)Z_{t+i}^{j\frac{\omega-1}{\omega}}\right]^{\frac{\omega}{\omega-1}}\right\}$$

where  $Z_{t+i}^{J}$  is a money aggregate defined as

$$Z_{t+i}^{j} = \left(\frac{M_{t+i}^{j}}{P_{t+i}}\right)^{1-\delta^{cs}} \left(\frac{D_{t+i}^{j} S_{t+i}}{P_{t+i}}\right)^{\delta^{cs}}$$

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In log linear form

$$u_{ct}^{CS} = u_{ct} - \Lambda\left(\omega\right) \left[\left(1 - \delta^{cs}\right) i_t + \delta^{cs} i_t^*\right]$$

MUC is affected by both domestic and foreign interest rate.

## Extension 2: Price dollarisation

$$\begin{array}{rcl} \pi_{Ht} & = & \left(1-\delta^{pd}\right)\pi_{s,t}+\delta^{pd}\left(\pi_{d,t}+ds_{t}\right)\\ \pi_{s,t}-\lambda_{\pi_{s}}\pi_{s,t-1} & = & \beta\left(E_{t}\pi_{s,t+1}-\lambda_{\pi_{s}}\pi_{s,t}\right)+\kappa_{S}\mathit{mc}_{t}^{D}\\ \pi_{d,t}-\lambda_{\pi_{d}}\pi_{d,t-1} & = & \beta\left(E_{t}\pi_{d,t+1}-\lambda_{\pi_{d}}\pi_{d,t}\right)+\kappa_{PD}\mathit{mc}_{t}^{S} \end{array}$$

• Increases the sensitivity of domestic inflation,  $\pi_{Ht}$  to the depreciation of the nominal exchange rate.

#### Extension 3:

#### Financial Dollarization

Entrepreneurs: expected real return of investing in capital

$$egin{split} E_t \left[ R_{t+1}^{ extit{KH}} 
ight] &= \left( 1 + extit{RP}_t 
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ight) rac{ extit{DS}_{t+1}}{\Pi_{t+1}} 
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Risk premium depends on debt relative to net worth:

$$RP_t = \left(\frac{D_t}{N_t}\right)^{\chi}$$

$$N_t = \left(R_t^{KH}\right) Q_{t-1} K_{t-1}$$

$$- \left(1 + RP_{t-1}\right) \left[ \left(\left(1 + i_{t-1}^*\right) \frac{DS_t}{\Pi_t}\right)^{\delta^{FD}} \left(\frac{1 + i_{t-1}}{\Pi_t}\right)^{1 - \delta^{FD}} \right] D_{t-1}$$

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#### Exchange rate intervention

Introduce a "backward looking" behavior in the exchange rate expectations:

$$egin{aligned} E_t^{\mathsf{exp}} s_{t+1} = \left(1 - \lambda_s
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The UIP becomes:

$$i_t - i_t^* = (1 - \lambda_s) \, extstyle E_t \Delta s_{t+1} - \lambda_s \Delta s_t + extstyle prem_t$$

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Iterate forward and solve for  $s_t$ :

$$s_t = s_{t-1} - rac{1}{\lambda_s} \sum_{j=0}^{\infty} \left(rac{1-\lambda_s}{\lambda_s}
ight)^j \left[i_{t+j} - i_{t+j}^* - extit{prem}_{t+j}
ight]$$

when 
$$\left\{egin{array}{ll} \lambda_s 
ightarrow 1: & s_t = s_{t-1} \ \lambda_s 
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ight.$$

## Data and Estimation

Sample 1995:01..2007:04. 10 observable variables

$$x_t = \ \left\{ \triangle c_t, \triangle y_t, \triangle \textit{inv}_t, \textit{rer}_t, \triangle s_t, \triangle \textit{tot}_t, i_t, i_t^*, \pi_t, \pi_t^m \right\}'$$

- 11 Shocks: One permanent global tech shock and 10 AR(1) shocks: technology, domestic inflation mark-up, intermediate imported mark-up, monetary, preference, foreign monetary policy, investment, UIP,PPP, and foreign technology.
- Unit root shock in the model. Consistency between data and model
- Nominal interest rate and inflation have been detrended considering the structural break (inflation target).

## Estimation

ullet Bayesian methods to estimate model s parameters  $(\Psi)$ 

Priors 
$$\Pi(\Psi)$$
 and Likelihood Function:  $L(\{x_t\}_{t=1}^T \mid \Psi)$ 

- Random-Walk Metropolis-Hastings algorithm to obtain 250,000 draws from the posterior distribution. (acceptation rate 0.25-0.35).
- From which we also obtain posterior second moments and impulse response functions.
- Compute the marginal likelihood of each model using the modified harmonic mean estimator.

## Result 1: Model Comparison

- Based on Bayes Factor: model with three types of dollarization dominates the rest of the models
- Main ingredient: financial dollarization.
- CS and PD do not add that much relative to FD.

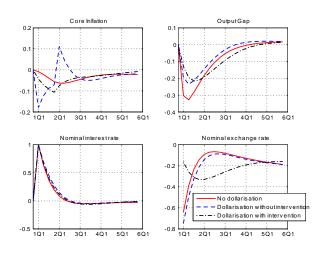
	Benchmark	CS	PD	FD	CS+PD+FD
Log-Marginal	-950.98	-948.61	-947.86	-945.32	-944.88

# Result 2: Parameter Estimates (CS+PD+FD)

- Real frictions are important in all models
- Prices are not that sticky. Firms change prices every 2 quarters.
- Price indexation is present:  $\lambda_P = 0.5$
- Relative large standard deviations of shocks (compared to developed economies)
- Elasticity of risk premium to Debt/Net worth ratio is similar to other studies ( $\chi=0.03$ )
- ullet Taylor Rule:  $arphi_\pi=$  2.29,  $arphi_y=$  0.26,  $arphi_s=$  0.80,  $arphi_i=$  0.06
- ullet Dollarization  $\delta^{cs}=0.46$  ,  $\delta^{pd}=0.12, \delta^{fd}=0.59$

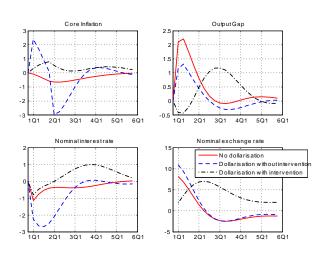
# Results: Transmission mechanism, contractive monetary policy shock.

Dollarisation counterfactual



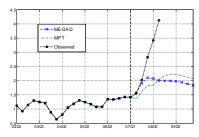
# Results: Transmission mechanism, increase in foreign interest rate.

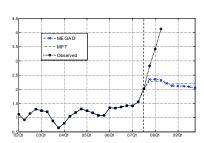
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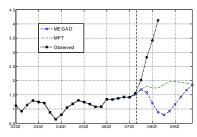


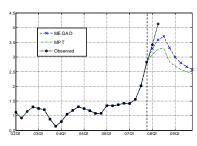
## Forecasting

#### First forecasting exercise with MEGA-D: CORE INFLATION (vintages 2007.I: 2007.IV)









## Concluding remarks and extensions

- The estimation and model evaluation validate the three forms of partial dollarization. However FD is the more important.
- Exchange rate intervention can help to ameliorate the effects of partial dollarization.
- Extensions for further work:
  - Include non-tradables goods (Balassa-Samuelson effect should be important).
  - Financial versus nominal frictions in emerging markets economices.
  - Dollarisaton as a endogenous decision (but this is problematic).
  - Change in policy regime.
  - Evaluate forecast